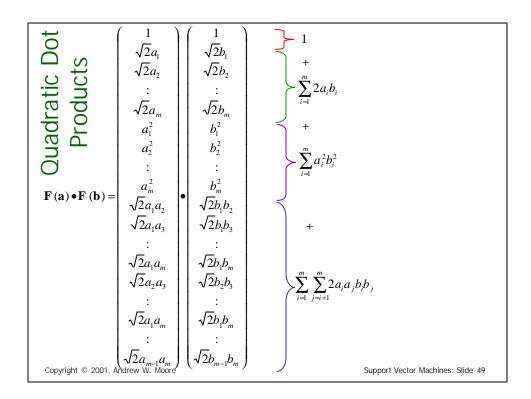
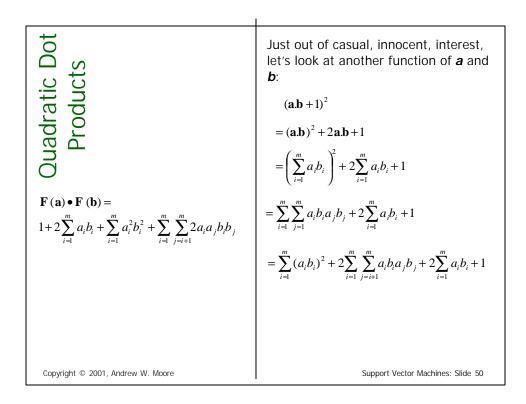
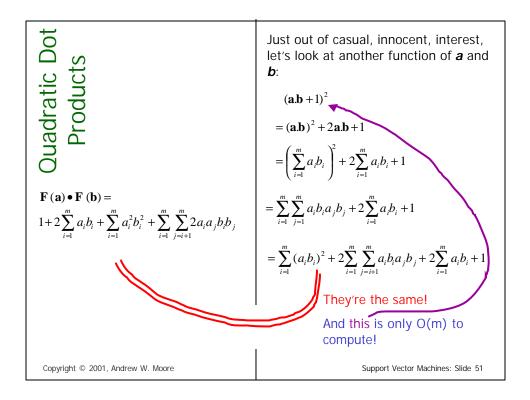


OP with bas	sis functions		
Maximize $\sum_{k=1}^{R} a_k + \sum_{k=1}^{R} \sum_{l=1}^{R} a_k a_l Q_k$	where $Q_{kl} = y_k y_l (\mathbf{F}(\mathbf{x}_k) \cdot \mathbf{F}(\mathbf{x}_l))$ We must do R <sup>2</sup> /2 dot products to		
Subject to these $0 \le a_k \le$ constraints:	get this matrix ready. Each dot product requires m <sup>2</sup> /2 additions and multiplications		
Then define:	The whole thing costs R <sup>2</sup> m <sup>2</sup> /4. Yeeks!		
$\mathbf{w} = \sum_{k \text{ s.t. } a_k} a_k y_k \mathbf{F} (\mathbf{x}_k)$ $b = y_K (1 - e_K) - \mathbf{x}_K \cdot \mathbf{w}$ where $K = \arg \max_k a$			
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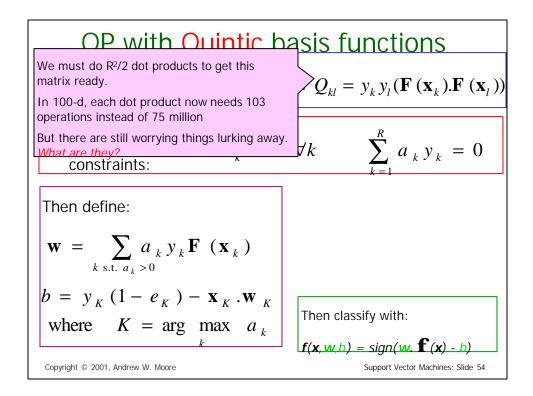


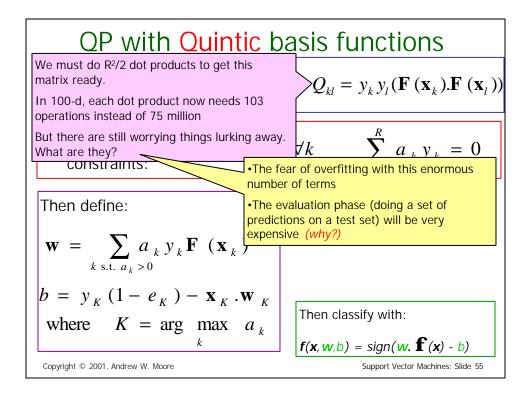


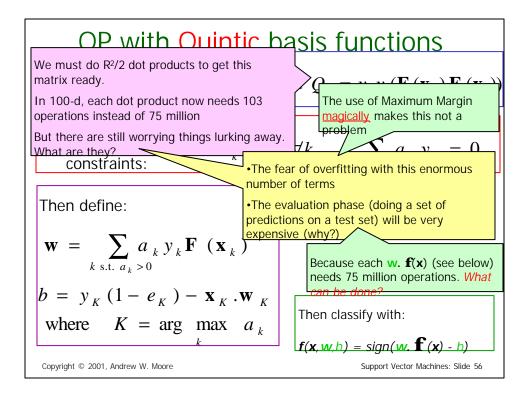


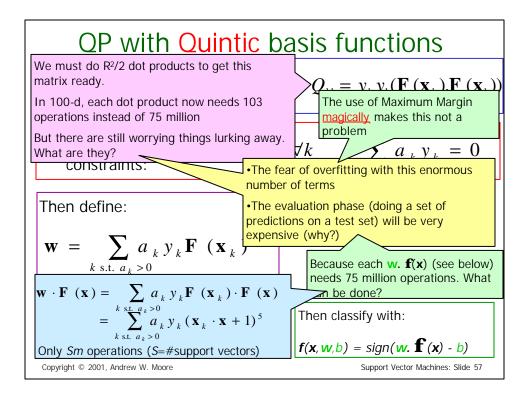
OP with Quadratic	basis functions
Subject to these $0 \le a_k \le \frac{ge}{Ea}$	where $Q_{kl} = y_k y_l (\mathbf{F}(\mathbf{x}_k).\mathbf{F}(\mathbf{x}_l))$ e must do R <sup>2</sup> /2 dot products to t this matrix ready. ch dot product now only requires additions and multiplications
Then define:	
$\mathbf{w} = \sum_{k \text{ s.t. } a_k > 0} a_k y_k \mathbf{F} (\mathbf{x}_k)$	Then classify with: f(x, w, b) = sign(w, f(x) - b)
$b = y_K (1 - e_K) - \mathbf{x}_K \cdot \mathbf{w}_K$	
where $K = \arg \max_{k} a_{k}$	
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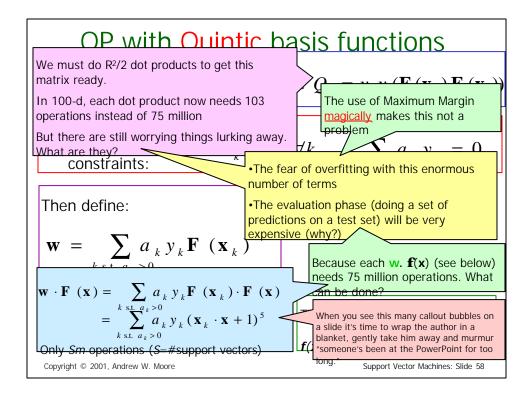
Higher Order Polynomials								
<b>f</b> (x)	Cost to build <i>Q<sub>k1</sub></i> matrix tradition ally	Cost if 100 inputs	<b>f</b> (a). <b>f</b> (b)	Cost to build <i>Q<sub>kI</sub></i> matrix sneakily	Cost if 100 inputs			
All <i>m<sup>2</sup>/2</i> terms up to degree 2	m <sup>2</sup> R <sup>2</sup> /4	2,500 <i>R</i> <sup>2</sup>	( <b>a</b> . <b>b</b> +1) <sup>2</sup>	m R <sup>2</sup> / 2	50 <i>R</i> <sup>2</sup>			
All <i>m<sup>3</sup>/6</i> terms up to degree 3	m <sup>3</sup> R <sup>2</sup> /12	83,000 <i>R</i> <sup>2</sup>	( <b>a</b> . <b>b</b> +1) <sup>3</sup>	m R <sup>2</sup> / 2	50 <i>R</i> <sup>2</sup>			
All <i>m<sup>4</sup>/24</i> terms up to degree 4	m <sup>4</sup> R <sup>2</sup> /48	1,960,000 <i>R</i> <sup>2</sup>	( <b>a</b> . <b>b</b> +1) <sup>4</sup>	m R <sup>2</sup> / 2	50 <i>R</i> <sup>2</sup>			
	<b>f</b> (x) All $m^2/2$ terms up to degree 2 All $m^3/6$ terms up to degree 3 All $m^4/24$ terms up to	$f(x)$ Cost to build $Q_{kl}$ matrix tradition allyAll $m^2/2$ terms up to degree 2 $m^2 R^2 / 4$ All $m^3/6$ terms up to degree 3 $m^3 R^2 / 12$ All $m^4/24$ terms up to $m^4 R^2 / 48$	$f(x)$ Cost to build $Q_{kl}$ matrix tradition allyCost if 100 inputsAll $m^2/2$ terms up to degree 2 $m^2 R^2 / 4$ $R^2 / 4$ 2,500 $R^2$ All $m^3/6$ terms up to degree 3 $m^3 R^2 / 12$ $R^2$ 83,000 $R^2$ All $m^4/24$ terms up to $m^4 R^2 / 48$ $R^2 / 48$ 1,960,000 $R^2$	$f(x)$ Cost to build $Q_{kl}$ matrix tradition allyCost if 100 inputs $f(a).f(b)$ All $m^2/2$ terms up to 	$f(x)$ Cost to build $Q_{kl}$ matrix tradition allyCost if 100 inputs $f(a).f(b)$ Cost to build $Q_{kl}$ matrix sneakilyAll $m^2/2$ terms up to degree 2 $m^2 R^2 / 4$ 2,500 $R^2$ $(a.b+1)^2$ $m R^2 / 2$ All $m^3/6$ terms up to degree 3 $m^3 R^2 / 12$ 83,000 $R^2$ $(a.b+1)^3$ $m R^2 / 2$ All $m^4/24$ terms up to $m^4 R^2 / 48$ 1,960,000 $R^2$ $(a.b+1)^4$ $m R^2 / 2$			

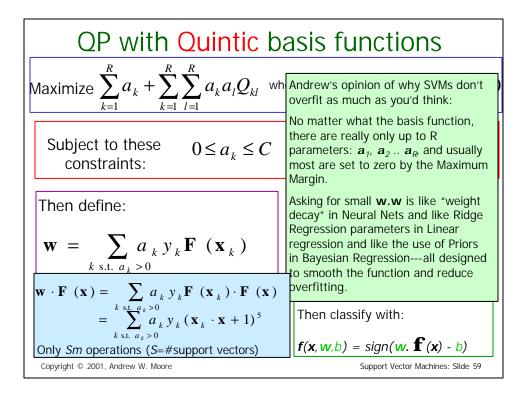


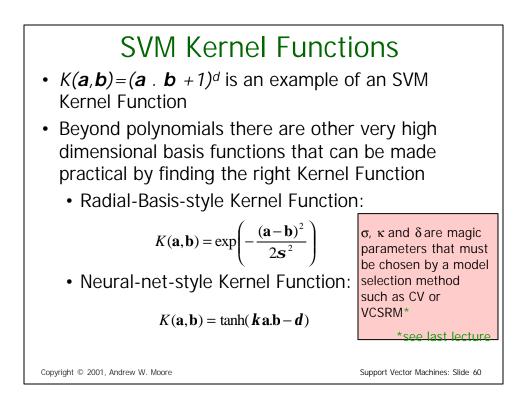


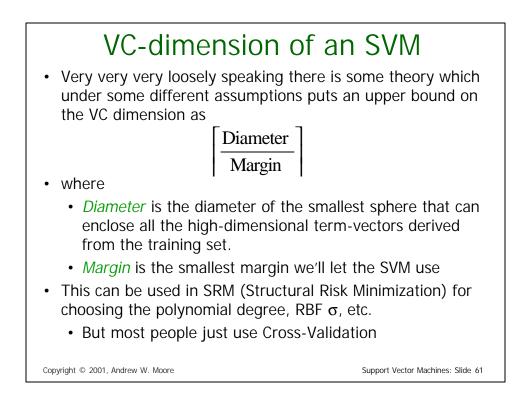


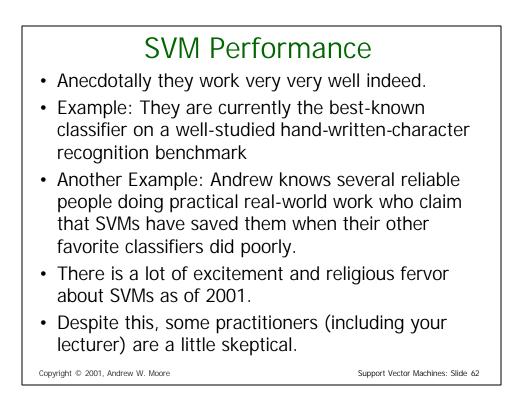


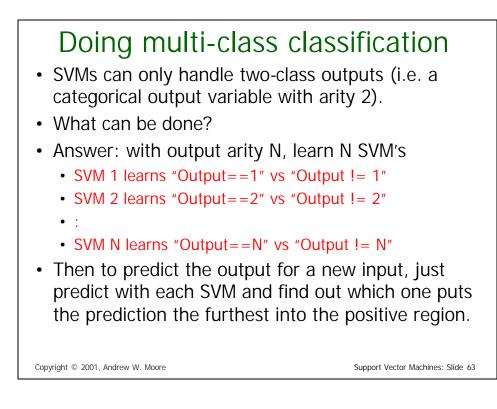


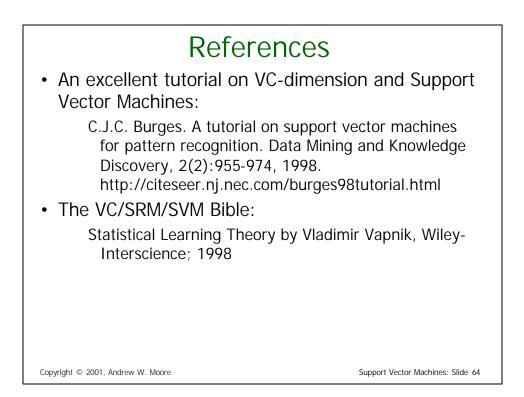












## What You Should Know

- Linear SVMs
- The definition of a maximum margin classifier
- What QP can do for you (but, for this class, you don't need to know how it does it)
- How Maximum Margin can be turned into a QP problem
- How we deal with noisy (non-separable) data
- How we permit non-linear boundaries
- How SVM Kernel functions permit us to pretend we're working with ultra-high-dimensional basisfunction terms

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