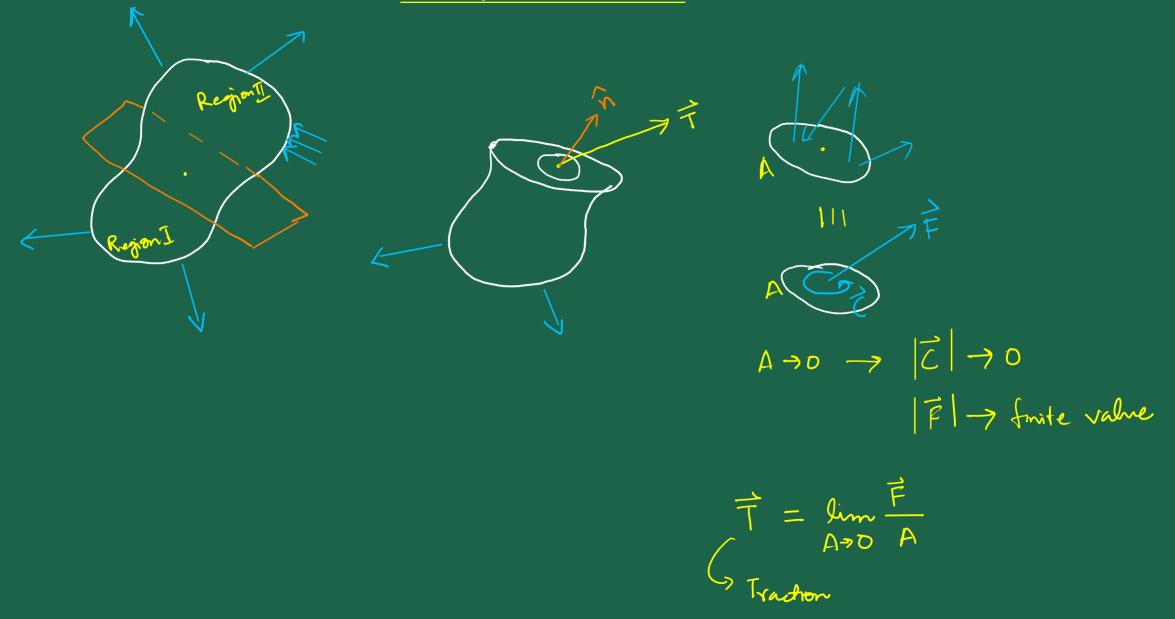
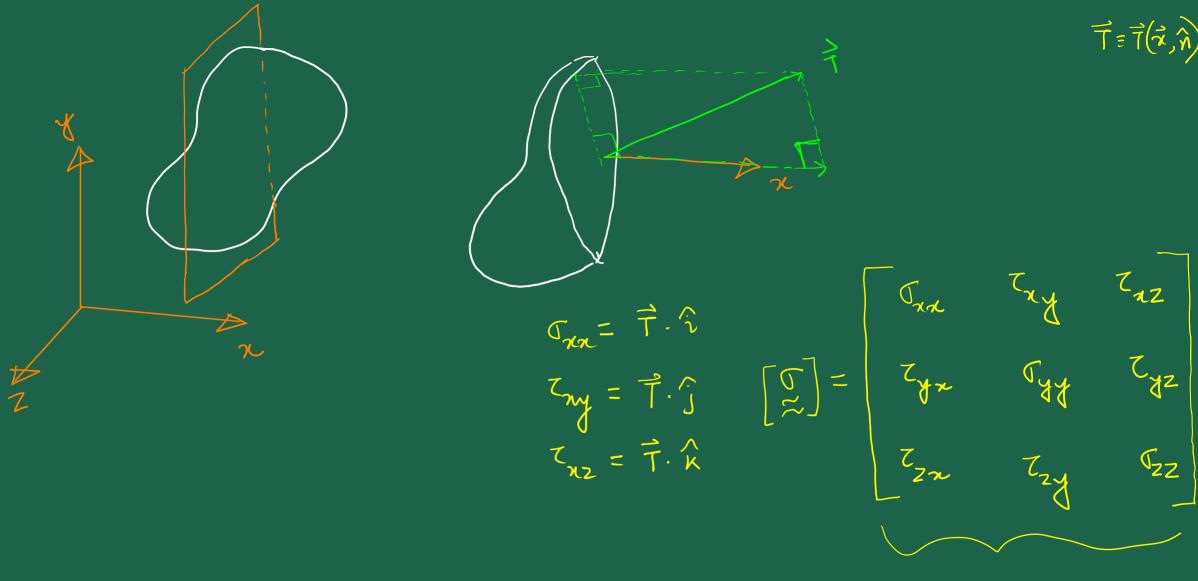
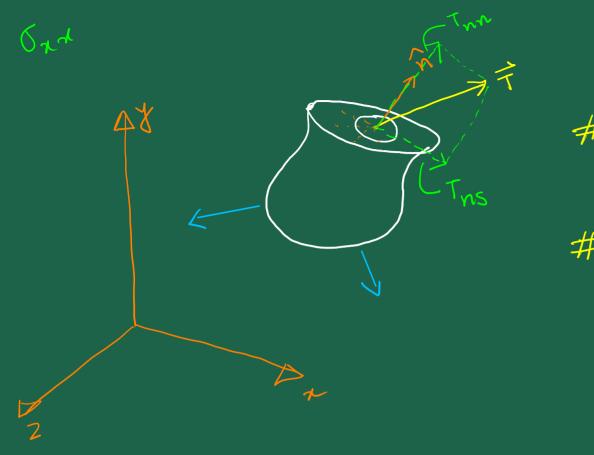
Concept of Traction

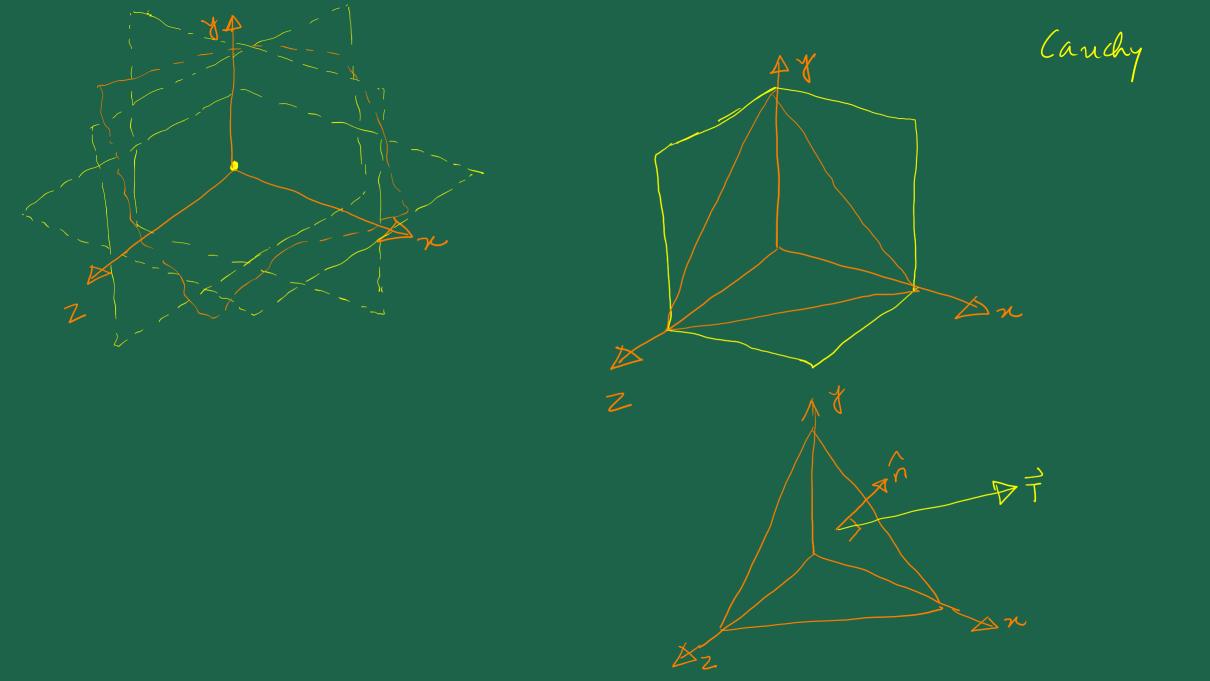


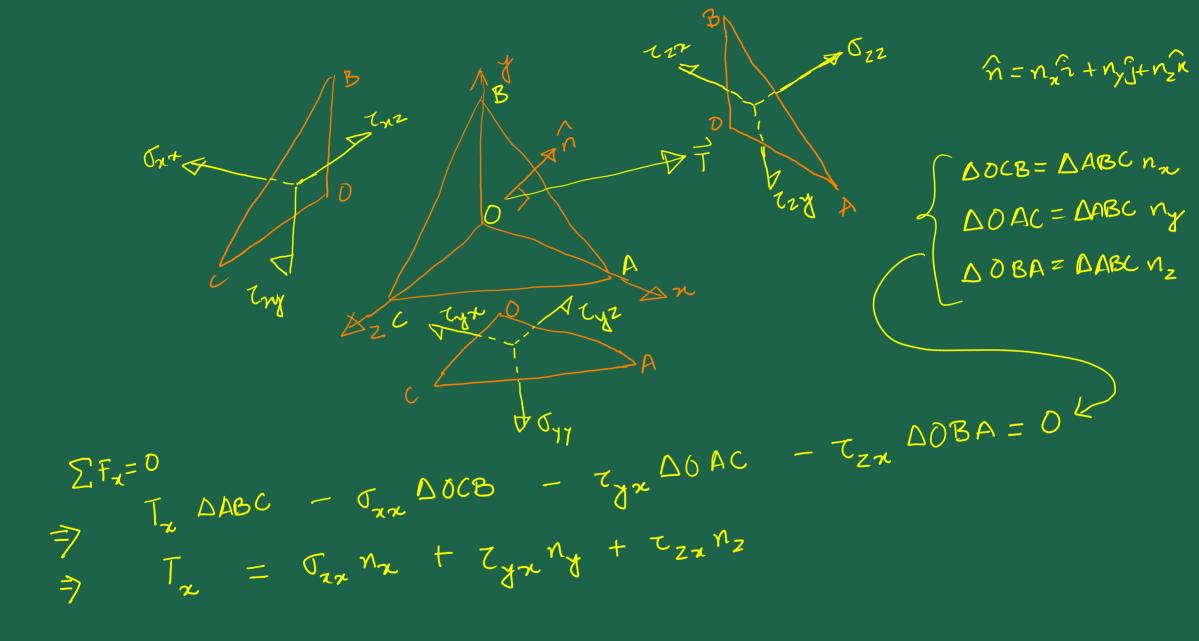


Strap tensor

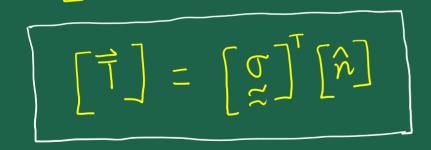


7 can be decomposed into two ways: $# = T_x \hat{i} + T_y \hat{j} + T_z \hat{k}$ # $\vec{T} = T_n \hat{n} + T_n \hat{e}_s$ € 1 n & ç is lying in the same plane containing 7 & n





ZFy=0 > Ty = Czynz + Cyyny + Czynz $\sum F_z = 0 \Rightarrow T_z = C_{xz} n_x + C_{yz} n_y + U_{zz} n_z$ $\begin{bmatrix} T_x \\ T_z \end{bmatrix} = \begin{bmatrix} \sigma_{xx} & \tau_{yx} & \tau_{zx} \\ \sigma_{yy} & \sigma_{yy} & \tau_{zy} \\ \sigma_{yz} & \sigma_{zz} & \sigma_{zz} \\ T_z \end{bmatrix} \begin{bmatrix} \tau_{xz} & \tau_{yz} & \sigma_{zz} \\ \sigma_{zz} & \sigma_{zz} \end{bmatrix} \begin{bmatrix} n_z \end{bmatrix}$



$$T_{nn} = \tilde{T} \cdot \hat{n}$$

$$\equiv [\tilde{T}]^{T}[\hat{n}]$$

$$= ([\tilde{\sigma}]^{T}[\hat{n}])^{T}[\hat{n}]$$

$$= [\tilde{n}]^{T}[\tilde{\sigma}][\hat{n}] \rightarrow \text{quadratic form}$$

Plane Stress
$$J_{zx} = J_{zy} = J_{zx} = 0$$

 $J_{zz} = J_{zy} = J_{zx} = 0$
 $J_{zx} = J_{zy} = J_{zx} = 0$
 $J_{zx} = J_{zy} = J_{zy} = J_{zy} = 0$
 $J_{zyx} = J_{yy} = J_{yy} = 0$
 $J_{zyx} = J_{yy} = J_{$

$$(T_{x}\hat{i} + T_{y}\hat{j} + T_{z}\hat{k}),$$

$$(n_{x}\hat{i} + n_{y}\hat{j} + n_{z}\hat{k}),$$

$$= T_{x}n_{x} + T_{y}n_{y} + T_{z}n_{z}$$

$$[T_{x}],$$

$$T_{y},$$

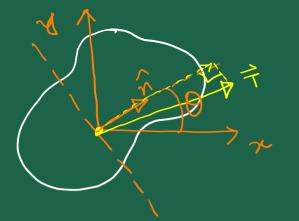
$$T_{y},$$

$$T_{z},$$

$$(A)(B),$$

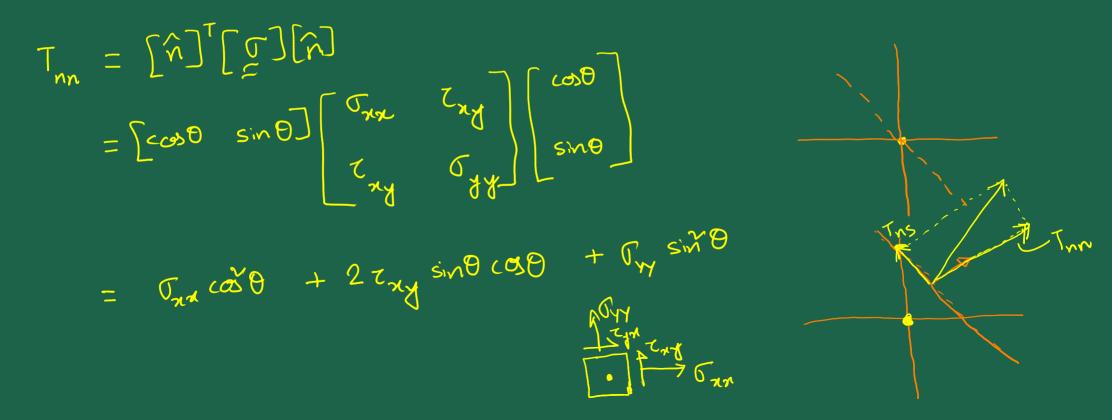
$$= (B)^{T}(A)$$

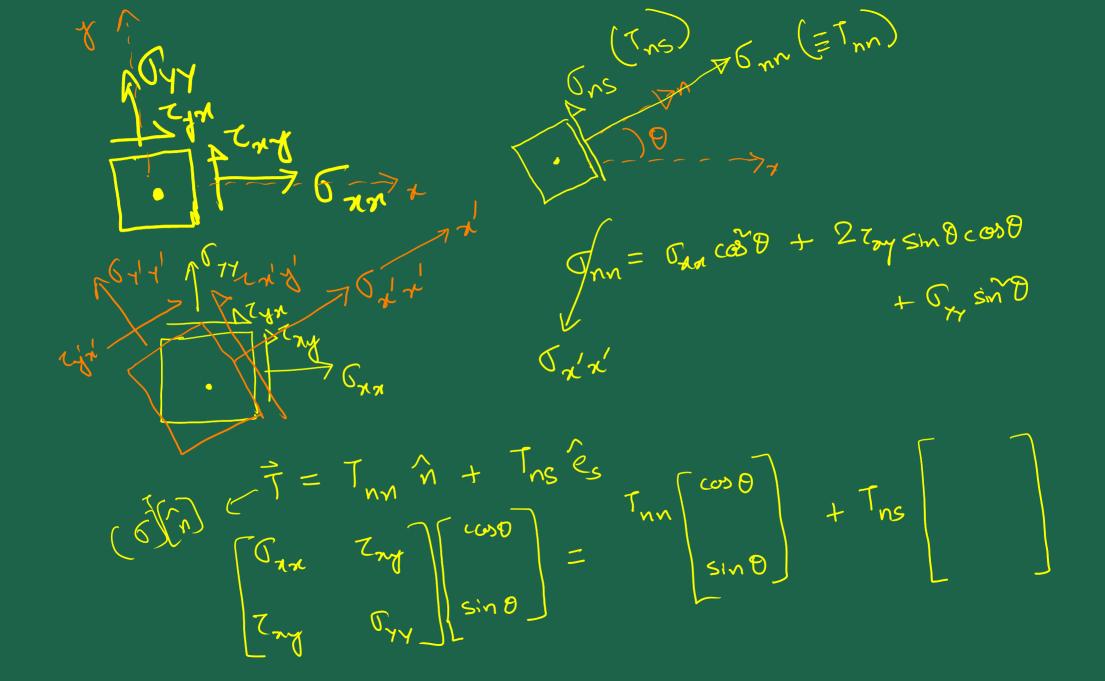
$$[x]^{T}(A)[n]$$





 $= \frac{n_{x} + n_{y}}{2}$ $= \cos\theta \hat{i} + \sin\theta \hat{j} \rightarrow [\hat{n}] = \left[\sin\theta \right]$ $= \sin\theta \hat{j} + \sin\theta \hat{j} - \frac{\sin\theta}{2} = \sin\theta \hat{j} + \sin\theta \hat{j} +$ $= n_x i + n_y j$





$$\begin{bmatrix} G_{xx} & Z_{nq} \\ T_{nq} & G_{yy} \end{bmatrix} \begin{bmatrix} \cos \theta \\ \sin \theta \end{bmatrix} = \begin{bmatrix} T_{nn} \\ \sin \theta \end{bmatrix} + T_{ns} \begin{bmatrix} -\sin \theta \\ \cos \theta \end{bmatrix}$$

$$\begin{bmatrix} G_{xx} & Z_{nq} \\ G_{yy} \end{bmatrix} \begin{bmatrix} \sin \theta \\ \sin \theta \end{bmatrix} = T_{nn} \cos \theta - T_{ns} \sin \theta = 0$$

$$G_{xx} \cos \theta + T_{xq} \sin \theta = T_{nn} \sin \theta + T_{ns} \cos \theta = 0$$

$$T_{nq} \cos \theta + G_{yy} \sin \theta = T_{nn} \sin \theta + T_{ns} \cos \theta = 0$$

$$E \lim \sin \theta = T_{nn} \sin \theta + T_{ns} \cosh \theta = 0$$

$$R \begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix}$$

$$\begin{bmatrix} \theta \\ -\cos \theta \end{bmatrix}$$

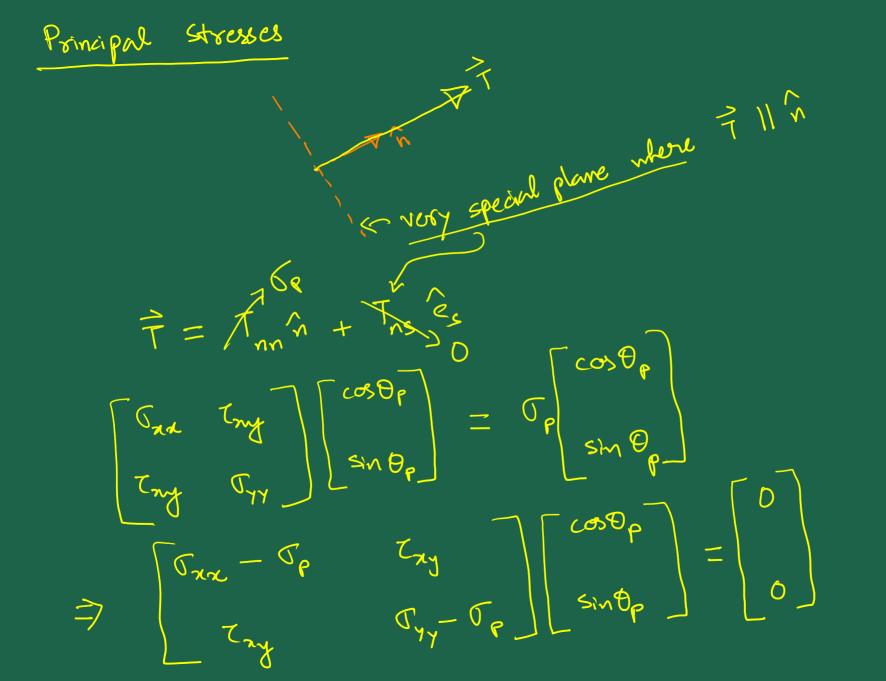
$$\begin{bmatrix} \sin \theta \\ -\cos \theta \end{bmatrix}$$

$$\int T_{ns} = T_{nq} (\cos \theta - \sin^{2} \theta) + (T_{y} - T_{xy}) \cos \theta \sin \theta$$

$$\begin{bmatrix} -\cos \theta \\ -\cos \theta \end{bmatrix}$$

 $\int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{Y}} \int_{\mathcal{Y}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{Y}} \int_{\mathcal{Y}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{Y}} \int_{\mathcal{Y}} \int_{\mathcal{Y}} \int_{\mathcal{X}} \int_{\mathcal{X}} \int_{\mathcal{Y}} \int$ $\zeta_{x'y'} = \zeta_{ny} \cos 2\theta - \frac{1}{2} \left(\mathcal{T}_{nx} - \mathcal{T}_{yy} \right) \sin 2\theta - \frac{\#}{2}$ $(\#_{1})^{2} + (\#_{2})^{2}$ $\frac{3}{2} \int \int dx' - \frac{1}{2} \left(\int_{xx} + \int_{yy} \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{xx} - \int_{yy} \int_{x'y'} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{xx} - \int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{xy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 = \frac{1}{4} \left(\int_{yy} \int_{yy} z \partial dy \right)^2 + z_{x'y'}^2 + z_{x'y'}^$ + (Jun - Ju) card Zrysin20 + \tilde{c}_{xy} $cos^2 20$ + $\frac{1}{4} \left(\tilde{c}_{xx} - \tilde{c}_{yy} \right) sm^2 20$ - Zny cos20 (Snn-Sy) sin20 $= \int \left(\int_{\mathbf{x}} \mathbf{x}' - \frac{1}{2} \left(\int_{\mathbf{x}} \mathbf{x}' + \int_{\mathbf{y}} \right)^2 + \int_{\mathbf{x}'}^2 \mathbf{y}' \right)$ $=\frac{1}{4}\left(\frac{\sigma_{xx}-\sigma_{yy}}{\tau}\right)+\tau_{xy}$

 $\int \overline{\mathcal{G}}_{x'x'} - \frac{1}{2} \left(\overline{\mathcal{G}}_{xx} + \overline{\mathcal{G}}_{yy} \right) + \overline{\mathcal{C}}_{x'y'} = \frac{1}{4} \left(\overline{\mathcal{G}}_{xx} - \overline{\mathcal{G}}_{yy} \right) + \overline{\mathcal{C}}_{yy}$ $7 \quad \left(\overline{J_{x'x'}} - \overline{J_{nvg}} \right)^2 + \overline{z_{x'y'}} = R^2, \qquad \left(\overline{J_{nn}} - \overline{J_{nvg}} \right)^2 + \overline{J_{nvg}}$ where $\overline{J_{nvg}} = \frac{1}{2} \left(\overline{J_{nn}} + \overline{J_{nvg}} \right)$ and $R = \sqrt{\left(\frac{\overline{J_{nn}} - \overline{J_{nvg}}}{2} \right)^2 + \overline{J_{nvg}}}$ This is in the forem of a circle ! This is in the forem of a circle ! This is in the forem of a circle ! This is in the forem of a circle ! This is in the forem of a circle ! This is in the forem of a circle ! ofto - Oman = Jang tR - Oman J J Mohre's Crecke Correct Frim (Jang, 0)

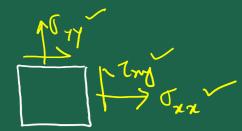


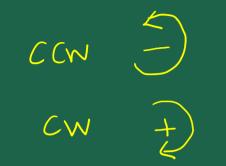
 $\begin{aligned}
 \sigma_{x,x} - \sigma_{\rho} & \zeta_{yy} \\
 \tau_{yy} & \sigma_{\gamma} - \sigma_{\rho}
 \end{aligned}$ = 0 $\sigma_{p} = (\sigma_{xx} + \sigma_{yy}) \pm (\sigma_{xx} - \sigma_{yy})^{2} + 4c_{xy}^{2}$ 2 $= \frac{\sigma_{xx} + \sigma_{yy}}{2} \pm \sqrt{\left(\frac{\sigma_{xx} - \sigma_{yy}}{2}\right) + \sigma_{xy}}$ R Jung = Javg t R

$$7 \quad Z_{xy} + G_{yy} \quad tom \Theta_{p} = G_{xx} \quad dem \Theta_{p} + Z_{xy} \quad tom \Theta_{p}$$
$$= (J_{xx} - G_{yy}) \quad tom \Theta_{p}$$
$$= (J_{xx} - G_{yy}) \quad tom \Theta_{p}$$

$$= \frac{2 \tan \theta \rho}{1 - \tan \theta \rho} = \frac{2 \cos \theta}{\ln \alpha - \cos \theta}$$

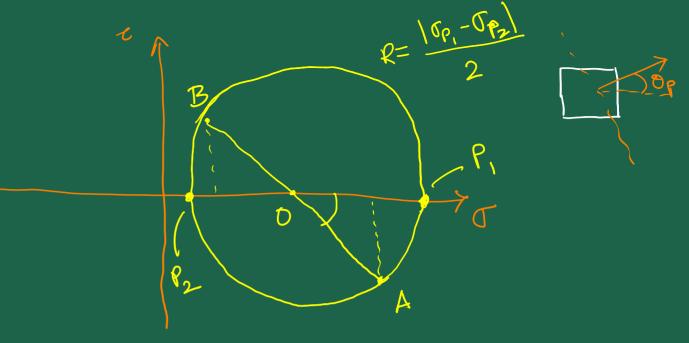
Max. margnitude of
$$T_{x'z'}$$
 is R. For the orientation of the plane:
 $T_{x'y'} = T_{xy} \cos 2\theta - \frac{1}{2} (T_{xx} - T_{yy}) \sin 2\theta$
 $\frac{d Z_{z'y'}}{d\theta} = 0$
 $\frac{d \theta}{d\theta} = 0$





A
$$\int G_{nn} = 20 MPa$$

 $Z_{ny} = 10 MPa$
 $\int G_{yy} = 5 MPa$
 $Z_{yy} = 10 MPa$
 $Z_{yy} = 10 MPa$



$$\tan (AOP_1) = \frac{c_{ny}}{\frac{1}{2}(G_{nn} - G_{yy})} = \frac{2 c_{ny}}{G_{nn} - G_{yy}}$$

Go back and dethethed

Max. in-plane shear stress =
$$R = \frac{|\sigma_{P_1} - \sigma_{P_2}|}{2}$$

Note: $\sigma_{ZZ} = 0$, $\sigma_{ZX} = 0$, $\sigma_{ZZ} = 0$
 $\sigma_{ZY} = \frac{|\sigma_{P_1} - \sigma_{P_2}|}{2}$
Note: $\sigma_{ZZ} = 0$, $\sigma_{ZX} = 0$, $\sigma_{ZZ} = 0$
 $\sigma_{ZY} = \frac{|\sigma_{P_1} - \sigma_{P_2}|}{2}$
Note: $\sigma_{ZZ} = 0$, $\sigma_{ZX} = 0$, $\sigma_{ZZ} = 0$
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