

## Lec 6

Last reminder: don't send emails regarding attendance. Instead, come to office hours for any mech issue about 'that' week's attendance.

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Partial derivatives of  $f(x, y)$ .

$$f: D \subseteq \mathbb{R}^2 \rightarrow \mathbb{R}$$

$$z = f(x, y), \quad (x, y) \in D.$$

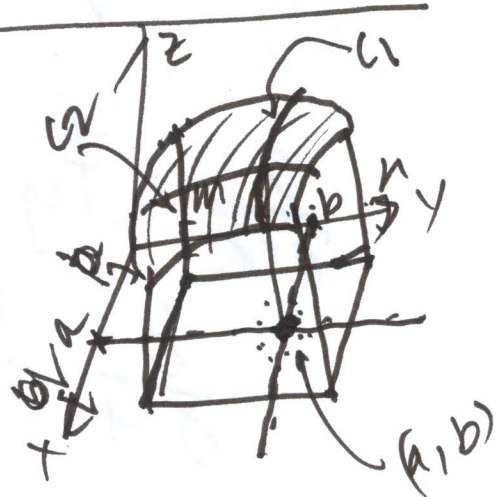
Local behavior of  $f(x, y)$  around  $(a, b) \in D$

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$$D = [a, b] \times [m, n]$$

Fixing  $y = b$ ,  $c_1 := f(x, b)$

$x = a$ ,  $c_2 := f(a, y)$



$$y = f(x)$$

$$\frac{dy}{dx} = f'(x)$$

$$\frac{d^2y}{dx^2} = f''(x) = \frac{d}{dx} f'(x)$$

For 2-variable fns -

$$f_x(x, y), f_y(x, y)$$

$$\frac{\partial}{\partial x} f_x(x, y) = f_{xx}(x, y)$$

$$\frac{\partial}{\partial y} f_x(x, y) = f_{yx}(x, y)$$

$$\frac{\partial}{\partial x} f_y(x, y) = f_{xy}(x, y)$$

$$\frac{\partial}{\partial y} f_y(x, y) = f_{yy}(x, y)$$

